

1. NO CALCULATORS ALLOWED

2. SHOW PROPER TO WORK TO RECEIVE FULL CREDIT

Find the focus of the parabola with equation $(y-3)^2 = -10(x+1)$. \rightarrow Negative is left

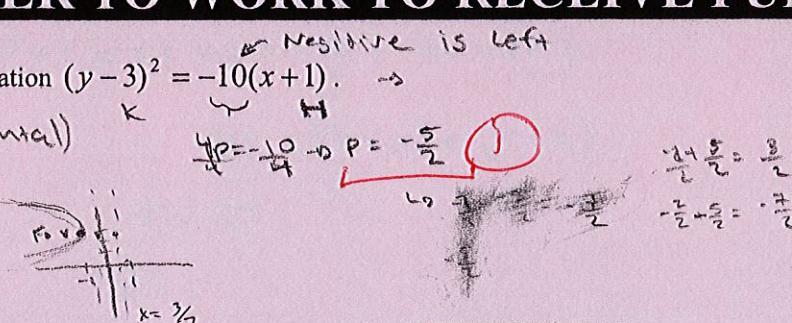
SCORE: 3 / 3 POINTS

$$\text{temp} \rightarrow y^2 = 4px \rightarrow \text{horizontal}$$

$$\text{vertex} = (-1, 3) \quad (1)$$

$$\text{focus} = (-\frac{7}{2}, 3)$$

$$\text{Directrix} x = x = \frac{3}{2}$$



$$\boxed{\text{FOCUS} = (-\frac{7}{2}, 3)} \quad (1)$$

Find the standard form of the equations of the parabolas with the following characteristics.

SCORE: 3 / 5 POINTS

[a] focus $(\frac{1}{2}, 0)$ and vertex $(0, 0)$ \rightarrow

$$\text{temp} = y^2 = 4px \rightarrow \text{vertical}$$

$$(x-0)^2 = 4(1/2)(y-0)$$

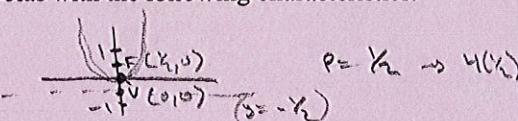
$$\rightarrow \boxed{x^2 = 2y} \quad (1)$$

[b] directrix $y = 6$ and vertex $(0, 0)$

$$\text{temp} = x^2 = 4py \rightarrow \text{vertical}$$

$$\text{vertex} = (0, 0)$$

$$\text{focus} = (0, -6)$$



$$(x-0)^2 = 24(y+0) \rightarrow \boxed{x^2 = -24y} \quad (1)$$

Find the standard form of the equation of the parabola with focus $(7, 6)$ and directrix $x = -1$.

SCORE: 5 / 6 POINTS

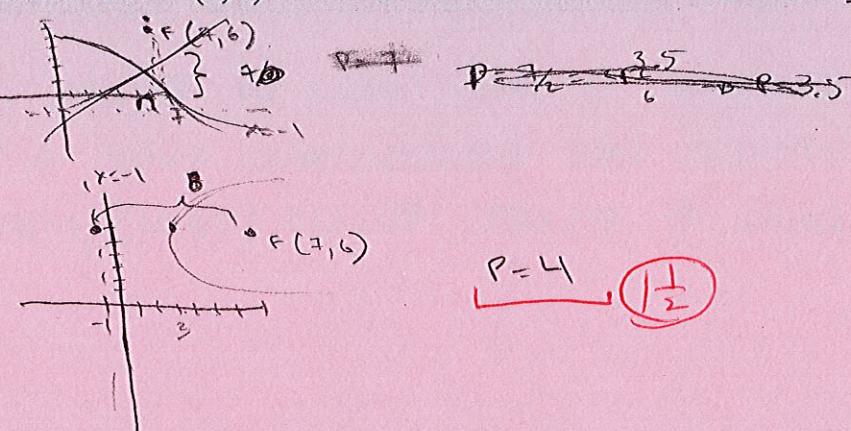
$$\text{Focus} = (7, 6)$$

$$\text{Directrix} = x = -1$$

$$\text{Vertex} = (\underline{\underline{\underline{}}})$$

$$\rightarrow (3, 6) \quad (1)$$

$$\boxed{(y-6)^2 = 16(x-3)} \quad (1)$$



$$P = 4 \quad (1)$$

Find the center and radius of the circle with equation $4x^2 + 4y^2 + 12x - 20y - 2 = 0$.

SCORE: ___ / 5 POINTS

$$\boxed{\text{Center} = (h, k)}$$

$$\boxed{\text{Center} = (-3, 5)}$$

$$\boxed{\text{radius} = \sqrt{35}}$$

$$4x^2 + 4y^2 + 12x - 20y - 2 = 0$$

$$\cancel{4x^2 + 4y^2} + 6x - 10y - 1 = 0$$

$$x^2 + \frac{6x}{2} + y^2 - \frac{10y}{2} = 1$$

$$x^2 + 6x + y^2 - 10y + 25 = 1 + 9 + 25$$

$$(x+3)^2 + (y-5)^2 = 35$$

$$r^2 = \sqrt{35}$$

$$r = \sqrt{35}$$

Write the standard form of the equation of the circle with center $(-4, 1)$ and solution point $(1, 3)$ (ie. the point lies on the circle).

SCORE: 3 / 3 POINTS

$$\boxed{\text{center} = (-h, k)}$$

$$(x-h)^2 + (y-k)^2 = r^2$$

$$\boxed{(1-(-4))^2 + (3-1)^2 = r^2} \quad \textcircled{1}$$

$$5^2 + 2^2 = r^2$$

$$25 + 4 = r^2$$

$$29 = r^2$$

\rightarrow

$$\boxed{(x+4)^2 + (y-1)^2 = 29}$$

$$\boxed{(x+4)^2 + (y-1)^2 = 29}$$

$$\boxed{\textcircled{1} \textcircled{2} \textcircled{3} \textcircled{4}}$$

Write the definition of a parabola. Use complete sentences and proper English as shown in lecture.

SCORE: 3 / 3 POINTS

A Parabola is the locus of points in the plane which are EQUIDISTANT from a fixed line (DIRECTRIX) AND A FIXED POINT (FOCUS), NOT ON THE LINE.